



1. 
$$f(x) = px^3 + 6x^2 + 12x + q.$$

Given that the remainder when  $f(x)$  is divided by  $(x - 1)$  is equal to the remainder when  $f(x)$  is divided by  $(2x + 1)$ ,

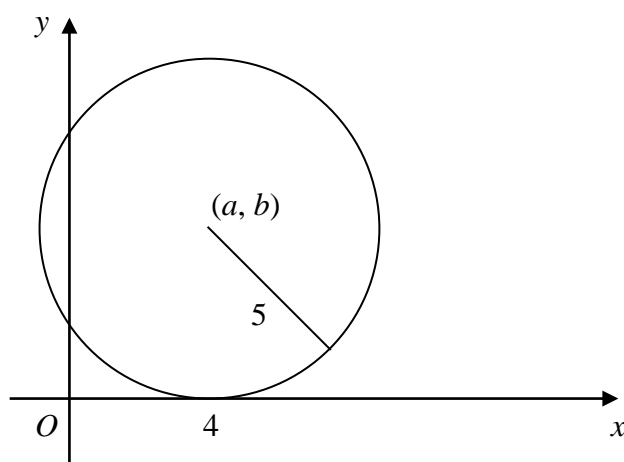
(a) find the value of  $p$ . (4 marks)

Given also that  $q = 3$ , and  $p$  has the value found in part (a),

(b) find the value of the remainder. (1 marks)

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2. Figure 1



The circle  $C$ , with centre  $(a, b)$  and radius 5, touches the  $x$ -axis at  $(4, 0)$ , as shown in Fig. 1.

(a) Write down the value of  $a$  and the value of  $b$ . (1 marks)

(b) Find a cartesian equation of  $C$ . (2 marks)

A tangent to the circle, drawn from the point  $P(8, 17)$ , touches the circle at  $T$ .

(c) Find, to 3 significant figures, the length of  $PT$ . (3 marks)

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3. (a) Expand  $(2\sqrt{x} + 3)^2$ . (2 marks)

(b) Hence evaluate  $\int_1^2 (2\sqrt{x} + 3)^2 dx$ , giving your answer in the form  $a + b\sqrt{2}$ , where  $a$  and  $b$  are integers. (5 marks)

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4. The first three terms in the expansion, in ascending powers of  $x$ , of  $(1 + px)^n$ , are  $1 - 18x + 36p^2x^2$ . Given that  $n$  is a positive integer, find the value of  $n$  and the value of  $p$ .

(7 marks)

5. Find all values of  $\theta$  in the interval  $0 \leq \theta < 360$  for which

(a)  $\cos(\theta + 75)^\circ = 0$ .

(3 marks)

(b)  $\sin 2\theta^\circ = 0.7$ , giving your answers to one decimal place.

(5 marks)

6. Given that  $\log_2 x = a$ , find, in terms of  $a$ , the simplest form of

(a)  $\log_2(16x)$ ,

(2 marks)

(b)  $\log_2\left(\frac{x^4}{2}\right)$ .

(3 marks)

- (c) Hence, or otherwise, solve

$$\log_2(16x) - \log_2\left(\frac{x^4}{2}\right) = \frac{1}{2},$$

giving your answer in its simplest surd form.

(4 marks)

7. The curve  $C$  has equation  $y = \cos\left(x + \frac{\pi}{4}\right)$ ,  $0 \leq x \leq 2\pi$ .

- (a) Sketch  $C$ .

(2 marks)

- (b) Write down the exact coordinates of the points at which  $C$  meets the coordinate axes.

(3 marks)

- (c) Solve, for  $x$  in the interval  $0 \leq x \leq 2\pi$ ,

$$\cos\left(x + \frac{\pi}{4}\right) = 0.5,$$

giving your answers in terms of  $\pi$ .

(4 marks)

8.

Figure 2

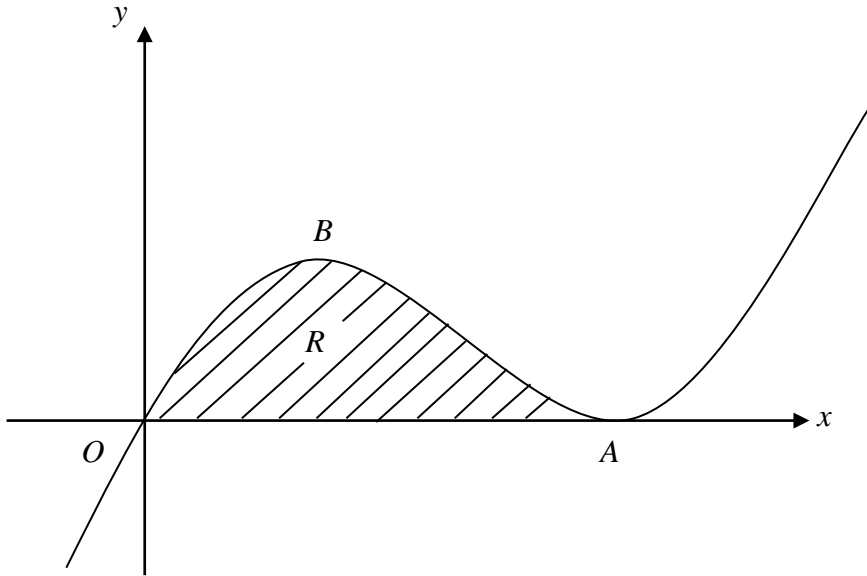


Figure 2 shows part of the curve with equation

$$y = x^3 - 6x^2 + 9x.$$

The curve touches the  $x$ -axis at  $A$  and has a maximum turning point at  $B$ .

(a) Show that the equation of the curve may be written as

$$y = x(x - 3)^2,$$

and hence write down the coordinates of  $A$ .

**(2 marks)**

(b) Find the coordinates of  $B$ .

**(5 marks)**

The shaded region  $R$  is bounded by the curve and the  $x$ -axis.

(c) Find the area of  $R$ .

**(5 marks)**

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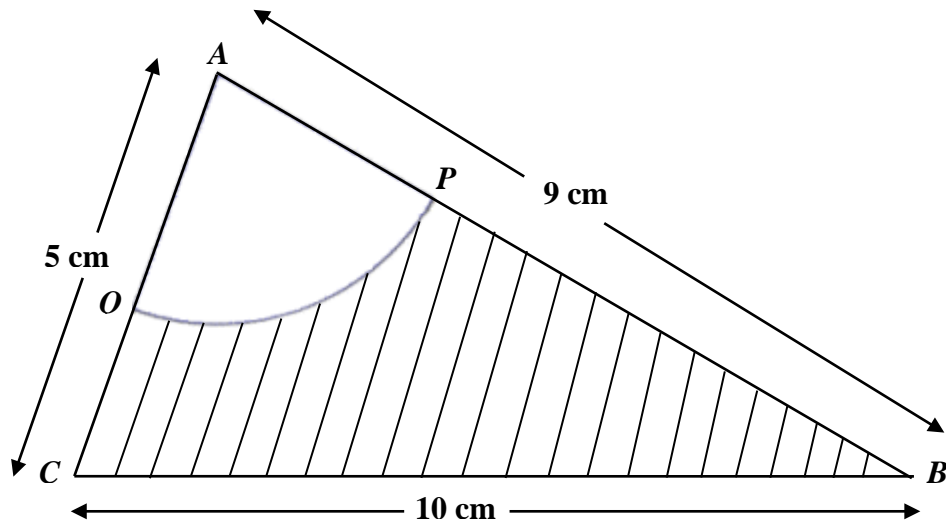


Fig. 3

Triangle  $ABC$  has  $AB = 9\text{ cm}$ ,  $BC = 10\text{ cm}$  and  $CA = 5\text{ cm}$ .

A circle, centre  $A$  and radius  $3\text{ cm}$ , intersects  $AB$  and  $AC$  at  $P$  and  $Q$  respectively, as shown in Fig. 3.

(a) Show that, to 3 decimal places,  $\angle BAC = 1.504$  radians. (3 marks)

Calculate,

(b) the area, in  $\text{cm}^2$ , of the sector  $APQ$ , (2 marks)

(c) the area, in  $\text{cm}^2$ , of the shaded region  $BPQC$ , (3 marks)

(d) the perimeter, in  $\text{cm}$ , of the shaded region  $BPQC$ . (4 marks)

END